## OCR Maths S1

# Topic Questions from Papers 

Representation of Data
Answers

| 1 (i) | Median 8 Quartiles 6, 24 | $\begin{array}{ll} \hline \text { B1 } & \\ \text { B2 } & 3 \end{array}$ | B1 for each Allow $\mathrm{IQR}=24-6$ |
| :---: | :---: | :---: | :---: |
| (ii) | Extreme values/skew distort mean or 35 mentioned | B1 $1$ | Accept just "data skewed". Not "anomaly" |
| (iii) | Advantage: retains data values Disadv: harder to read (eg) median harder to compare distr's visual comparison harder | B1 <br> B1 <br> 2 | Not "Can be shown on same diag" |


| 2 (i) Read at 300 or 300.25 and 900 or 900.75 44.5 to 45.5 and 69 to 69.9 IQR 23.5 to 25.4 | M1  <br> A1  <br> A1 3 | or 44-46 and 68-70 incl. <br> dep A1 Must look back, see method. No wking, ans in range: M1A1A1 |
| :---: | :---: | :---: |
| $\begin{aligned} & \text { (ii) } 0.6 \text { or } 60 \% \\ & \text { CF } 720 \\ & 63 \text { to } 64 \end{aligned}$ | $\begin{array}{ll} \text { M1 } & \\ \text { M1 } & \\ \text { A1 } & 3 \end{array}$ | Seen or implied <br> Seen or implied $55.5 \text { to 56: SC B1 }$ |
| $\begin{aligned} & \text { (iii) } 1200-860 \\ & =340 \end{aligned}$ | $\begin{array}{ll} \text { M1 } \\ \text { A1 } \end{array}$ | $\begin{aligned} & \text { Allow } 1200 \text { - }(850 \text { to } 890) \\ & 310 \text { to } 350 \end{aligned}$ |
| $\begin{aligned} & \text { (iv) } 340 / 1200 \\ & 0.283^{5} \\ & =0.00183 \end{aligned}$ | M1 <br> M1dep <br> A1 $3$ | their (iii)/1200 <br> [their (iii)/1200] ${ }^{5}$ exactly <br> Allow 0.00114 to $0.00212 \geq 2 \mathrm{sfs}$ |
|  |  | ${ }^{340} \mathrm{C}_{5} 1^{1200} \mathrm{C}_{5} \ldots \mathrm{M} 1$ |
| (v) Incorrect reason or ambiguity: B0B0. Otherwise: <br> Too low, or should be 26 or 27 or 2 or 3 higher | B2 2 | eg $\mathrm{IQR}=55-35=20$ or $\mathrm{IQR}=$ value $>27$ <br> or new info' implies straight line: B1 or originally, majority in range $35-55$ are at top of <br> this range: B 1 |
|  | 13 |  |

(Q5, June 2005)

| 3 (i) | Midpoints attempted $\quad \geq 2$ classes $\sum x f / 100$ or $\sum x f / \sum f$ attempted $x$ within class, not class width Mean $=27.2$ (to 3 sfs $\quad$ (not 27.25) art 27.2 from fully correct wking | M1 M1 <br> A1 <br> M1 <br> M1 <br> A1 $6$ | Correct (149.5) <br> 2720.5/100 <br> 27.2 <br> 240702.25 <br> 40.82 <br> allow class width | With 150 <br> 2725/100 <br> 27.25 <br> 242050 <br> 40.96 <br> or 2nd M1 | $\begin{aligned} & \underline{\underline{T o t}=} \\ & \underline{2000} \\ & \text { Allow } \\ & \text { Ms } \\ & \text { \& poss } \\ & \text { As } \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| (ii) | Recog LQ in $1^{\text {st }}$ class $\underline{\&} \mathrm{UQ}$ in $3^{\text {rd }}$ class <br> Subtract $\mathrm{IQR}=23 \text { or } 24 \text { or } 25$ | M1 <br> M1 <br> A1 <br> 4 | both nec' $y$ <br> dep B1or M1 <br> integer. dep M2 |  |  |
| $\begin{array}{r} \text { (iii)(a) } \\ \text { (b) } \\ \text { (c) } \\ \hline \end{array}$ | Increase Increase No change |   <br> B1 $\mathbf{1}$ <br> B1 $\mathbf{1}$ <br> B1 $\mathbf{1}$ | Ignore "probably" etc |  |  |
| Total |  | 13 |  |  |  |

(Q7, June 2006)

| 4 (ia) | W \& Y oe | B1 1 |  |
| :---: | :---: | :---: | :---: |
| b | X oe | B1 1 |  |
| ii | Geo probs always decrease <br> or Geo has no upper limit to $x$ or $x \neq 0$ | B1 1 | Geo not fixed no. of values diags have fixed no of trials not Geo has + ve skew |
| iii | W <br> Bin probs cannot fall then rise or bimodal | B1 B1dep 2 | indep <br> allow Bin probs rise then fall |
| Total |  | 5 |  |


| 5 (i) | $\begin{aligned} & \mathrm{Med}=2 \\ & \mathrm{LQ}=1 \text { or } \mathrm{UQ}=4 \\ & \mathrm{IQR}=3 \end{aligned}$ | $\begin{array}{ll} \hline \text { B1 } & \\ \text { M1 } \\ & \\ \text { A1 } & 3 \end{array}$ | ```cao or if treat as cont data: read cf curve or interp at 25 & 75 cao``` |
| :---: | :---: | :---: | :---: |
| ii | Assume last value $=7$ (or eg 7.5 or 8 or 8.5 ) <br> $x f$ attempted $\geq 5$ terms <br> 2.6 or 3 sf ans that rounds to 2.6 $x^{2} f$ or $\left.\quad . x-m\right)^{2} f \quad \geq 5$ terms $V\left(x^{2} f / 100-m^{2}\right)$ or <br> $V\left((. x-m)^{2} f\right) / 100$ fully correct but $\mathrm{ft} m$ <br> 1.6 or 1.7 or 3 sf ans that rounds to 1.6 or 1.7 | B | stated, \& not contradicted in wking eg 7-9 or 7,8, 9 Not just in wking allow "midpts" in $x f$ or $x^{2} f$ <br> dep M3 <br> penalize > 3 sfs only once |
| iii | Median less affected by extremes or outliers etc (NOT anomalies) | B1 | or median is an integer or mean not int. or not affected by open-ended interval general comment acceptable |
| iv | Small change in var'n leads to loe change in IQR UQ for W only just 4 , hence IQR exaggerated orig data shows variations are similar | B1 | for Old Moat LQ only just 1 \& UQ only just 3 oe ...... specific comment essential |
| v | OM \% (or $y$ ) decr (as $x$ incr) oe Old Moat | $\begin{array}{ll} \text { B1 } \\ \text { B1 } & 2 \end{array}$ | ranks reversed in OM or not rev in W NIS |
| Total |  | 13 |  |

(Q8, Jan 2007)

| 6 (i) | $\begin{aligned} & 1991 \\ & 100000 \text { to } 110000 \end{aligned}$ | B1 ind B1 ind 2 | Or fewer in 2001 <br> Allow digits100 to 110 |
| :---: | :---: | :---: | :---: |
| iia | $\begin{aligned} & \text { Median }=29 \text { to } 29.9 \\ & \text { Quartiles } 33 \text { to } 34,24.5 \text { to } 26 \\ & =7.5 \text { to } 9.5 \\ & 140 \text { to } 155 \\ & 23 \text { to } 26.3 \% \end{aligned}$ | B1 M1 A1 M1 A1 5 | Or one correct quartile and subtr <br> NOT from incorrect wking <br> $\times 1000$, but allow without <br> Rnded to 1 dp or integer 73.7 to $77 \%$ : SC1 |
| b | Older <br> Median (or ave) greater $\quad\}$ <br> \% older mothers greater oe\} <br> \% younger mothers less oe\} | $\begin{array}{ll} \text { B1 } & \\ \text { B1 } & \\ \text { B1 } & 3 \end{array}$ | Or 1991 younger <br> Any two Or 1991 steeper so more younger: B2 NOT mean gter Ignore extra |
| Total |  | 10 |  |

(Q5, June 2007)

(Q8, Jan 2008)

| 8 (i) | $\begin{aligned} & 25 / 10 \\ & =2.5 \end{aligned}$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } 2 \end{aligned}$ | Allow ${ }^{25} /_{(9 \text { tol0) }}$ or 2.78: M1 |
| :---: | :---: | :---: | :---: |
| ii | $\begin{aligned} & (19.5,25) \\ & (9.5,0) \end{aligned}$ | $\begin{aligned} & \text { B1 } \\ & \text { B1 } 2 \end{aligned}$ | Allow (24.5, 47) <br> Both reversed: SC B1 <br> If three given, ignore $(24.5,47)$ |
| iii | Don't know exact or specific values of $x$ (or min or max or quartiles or median or whiskers). <br> Can only estimate (min or max or quartiles or median or whiskers) oe Can't work out (.....) Data is grouped oe | B1 1 | Exact data not known <br> Allow because data is rounded |
| Total |  | 5 |  |


| 9 (i) | $\begin{aligned} & \hline 68 \\ & 75-59 \\ & =16 \\ & \hline \end{aligned}$ | B1 <br> M1 <br> A1 3 | attempt $6^{\text {th }} \& 18^{\text {th }}$ or $58-60,74-76 \&$ subtr must be from $75-59$ |
| :---: | :---: | :---: | :---: |
| (ii) | Unaffected by outliers or extremes <br> (allow less affected by outliers) sd can be skewed by one value | B1 1 | NOT: ... by anomalies or freaks easier to calculate |
| (iii) | Shows each data item, retains orig data can see how many data items can find (or easier to read) mode or modal class can find (or easier to read) frequs can find mean <br> Harder to read med (or Qs or IQR) Doesn't show med (or Qs or IQR) B\&W shows med (or Qs or IQR) B\&W easier to compare meds | B1 $\text { B1 } 2$ | NOT: shows freqs <br> shows results more clearly <br> B\&W does not show freqs <br> NOT: B\&W easier to compare <br> B\&W shows spread or variance or skew B\&W shows highest \& lowest <br> Assume in order: Adv, Disadv, unless told Allow disadv of B\&W for adv of S\&L $\&$ vice versa <br> Ignore extras |
| (iv) | $\mathrm{m}=68.1$ NOT by restart <br> $\mathrm{sd}=9.7$ (or same) NOT by restart | $\begin{array}{ll} \text { B1 } & \\ \text { B1 } & 2 \end{array}$ | Restart mean or mean \& sd: <br> 68.1 or $68.087 \& 9.7$ or 9.73 B1 only |
| Total |  | 8 |  |

(Q5, Jan 2009)

| 10 (i) (a) | $\begin{array}{lr} \text { Use of correct midpts } & \\ \Sigma l f \div \Sigma f & (=706 \div 40) \\ =17.65 & \\ \Sigma l^{2} f & (=13050.5) \\ \sqrt{\frac{13050.5 "}{40}-17.655^{22}} & (=\sqrt{ } 14.74) \\ =3.84(3 \mathrm{sfs}) & \end{array}$ | B1 <br> M1 <br> A1 <br> M1 <br> M1 <br> A1 $6$ | 11,14,18,25.5 <br> $l$ within class, $\geq$ three lf seen <br> [17.575,17.7] <br> $\geq$ three $l^{2} f$ seen <br> $\div 40,-$ mean $^{2}, \sqrt{ }$. Dep $>0$. <br> $\sum(1-17.65)^{2 f}$, at least $3 \mathrm{M} 1, \div 40, \sqrt{ }$ <br> M1,3.84 A1. <br> $\div 4 \Rightarrow \max$ B1M0A0M1M0A0 |
| :---: | :---: | :---: | :---: |
| (b) | mid pts used or data grouped or exact values unknown oe | B1 1 | not "orig values were guesses" |
| (ii) | $\begin{aligned} & 20 \div 5 \\ & =4 \end{aligned}$ | $\begin{array}{ll} \text { M1 } \\ \text { A1 } & 2 \end{array}$ | condone $20 \div[4,5]$ or ans 5 |
| (iii) | $\begin{aligned} & 20.5^{\text {in }} \text { value requ'd and } \\ & 1^{\text {st }} \text { two classes contain } 14 \text { values } \\ & 16-20 \end{aligned}$ | $\begin{aligned} & \text { M1 } \\ & \text { B1 } 2 \end{aligned}$ | condone $20^{\mathrm{Th}}$ oe or third class oe |
| (iv) (a) | increase | B1 1 |  |
| (b) | decrease | B1 1 |  |
| Total |  | [13] |  |


(Q6, Jan 2013)

| 12 (i) | 590 | B1 1 | Allow approximately 590 |
| :---: | :---: | :---: | :---: |
| ii | Graph horiz (for $\geq 55 \mathrm{mks}$ ) oe | B1 1 | or levels off, or grad $=0$, grad not increase Allow line not rise, goes flat, plateaus, stops increasing, not increase, doesn't move |
| iii | 39 to 41 | B1 1 |  |
| iv | Attempt read cf at 26 or 27 Double \& attempt read $x$ <br> Max C=29 to 31.5 | M1 M1 <br> A1 3 | eg $26 \mathrm{mks} \rightarrow 150^{\text {it }} \quad 27 \mathrm{mks} \rightarrow 180^{1 \mathrm{~h}}$ <br> eg read at $\mathrm{cf}=300$ or 360 Indep of first M1 <br> May be implied by ans <br> Answer within range, no working, M1M1A1 <br> 32 without working, sc B1 |
| v | $\begin{aligned} & \mathrm{LQ}=25.5-26.5 \text { or } \mathrm{UQ}=34-35.5 \\ & \mathrm{IQR}=8-10 \end{aligned}$ <br> (German) more spread | M1 <br> A1 <br> B1ft 3 | M1 for one correct quartile dep $\geq 1$ correct quartile or no working <br> or less consistent, less uniform, less similar, more varied, more variable, greater variance, more spaced apart, further apart ft their IQR; must be consistent with IQR <br> Correct comment with no working: M0A0B1 |
| Total |  | 9 |  |


| 13 (i) | $\begin{array}{\|l\|} \hline 38 \\ 61 \\ \hline \end{array}$ | $\begin{array}{ll} \hline \text { B1 } & \\ \text { B1 } & 2 \end{array}$ | Reversed: B1B0 |  |
| :---: | :---: | :---: | :---: | :---: |
| ii | Paper 2 <br> Higher median or curve is to right | B1 <br> B1dep 2 | Indep of reason <br> or similar <br> Higher average or mean or midpoint <br> Paper 2: half $\leq 61$, cf paper 1 : half $\leq 38$ <br> Paper 1: more students scored lower marks (or lower than eg 40) | Ans "Paper 1", ignore reason: B0B0 unless reversed in (i) <br> More scored higher mks <br> Highest \& lowest mks are higher <br> For each cf, the corresponding mark is higher in p2. <br> None get 0-10 <br> Some get 100 <br> Eg 25 scored > 69 in p1, cf 65 scored > 69 in p2 <br> NOT Marks are higher NOT marks seem higher <br> NOT everyone gets higher mks <br> NOT Curve steeper <br> Ignore irrelevant or incorrect <br> SC: If reversed in (i): (ii) p1 because median higher B1B1ft |
| iii | 55,25 <br> 73, 46 <br> Paper $1 \mathrm{IQR}=30$ <br> Paper $2 \mathrm{IQR}=27$ <br> Suggestion correct or p2 less varied | M1 <br> A1 <br> A1 <br> B1f <br> indep | M1 one pair of quartiles <br> p2 more consistent or less spread out Allow "p2 has smaller range (or smaller variance") if IQRs found <br> "It" is less varied: assume p2: B1 | Allow $55 \pm 1,25 \pm 1 \quad$ Not necessarily subtracted  <br> $73 \pm 1,46 \pm 1$  <br>   <br> $20 \pm 1$  <br> $27 \pm 1$  <br> p1 more varied or more spread out or less consistent Little difference or similarly varied <br> NOT p2 IQR smaller than p1 unless also says less varied oe <br> If quartiles found but not IQRs: max M1A0A0B1 <br> If no quartiles calculated can still score B1 <br> Steeper curve alone <br> M0A0A0B0 <br> If IQRs wrong, with $\mathrm{p} 1<\mathrm{p} 2$, ft "suggestion wrong": B1f <br> Ignore irrelevant or incorrect |
| iv | $37( \pm 3)$ | B2 2 | B1 for $163( \pm 3)$ | Not necessarily integer. <br> B1 for 78-80 mks for min grade A on p2 <br> SC: ans 105-110: B1 (from p1 10 mks hier instead of lower) |
| v | $\begin{aligned} & 37.5 \\ & 28.2 \end{aligned}$ | $\begin{array}{ll} \hline \text { B1 } & \\ \text { B1 } & 2 \\ \hline \end{array}$ | cao or sd the same | NOT eg 37.51 <br> Ignore all working |
| Total |  | 12 |  |  |


| 14 (i) | Method is either: Just $4 \div 3$ or $\frac{4}{3}$ or: Use of ratio of correct frequencies AND ratio of widths (correct or 4 and 2) |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | $5.6 \times \frac{4}{28} \times \frac{5}{3}$ or $0.8 \times \frac{5}{3}$ <br> or $\left(5.6 \div \frac{28}{5}\right) \times \frac{4}{3} \quad$ or $\frac{4}{3}$ or $4 \div 3 \quad$ oe $=1 \frac{1}{3}$ or $\frac{4}{3}$ or $1.33(3 \mathrm{sf})$ oe | M2 <br> A1 3 | M1 for $5.6 \times \frac{4}{28} \times \frac{4}{2}$ or $0.8 \times \frac{4}{2}$ <br> or $\left(5.6 \div \frac{28}{4}\right) \times \frac{4}{2} \quad$ or $0.8 \times 2 \quad$ oe $\quad(=1.6)$ <br> No wking, ans 1.3: M2A0 <br> Ans 1.6: Check wking but probably M1M0A0 | Correct calc'n using 5.6, 28, $4,5,3$ oe: M2 Correct calc'n using 5.6, 28, 4, 4, 2 oe: M1 <br> ie fully correct method: M2 <br> or: incorrect class widths, otherwise correct method: M1 <br> $\frac{4}{3}$ correctly obtained (or no wking) then further incorrect: <br> M1M0A0 <br> Use of ratio of widths OR freqs but not both: M0 eg $5.6 \times \frac{4}{28}(=0.8)$ or $5.6 \times \frac{3}{5}(=3.36): \quad$ M0 $\frac{4}{2}=2: \text { M0M0A0 }$ |
| ii | 25 or 26 or 25.5 <br> Med is $21^{\text {st }}$ (or $22^{\text {nd }}$ or $21.5^{\text {th }}$ ) in 31-35 class or "25-4" <br> Can be implied by calc' $n$ <br> Med > 33 or "more than" | B1 <br> B1 $\text { B1 } 3$ | or $25 \& 26$ <br> or med in last $\approx 7$ in class or $33 \approx 14^{\text {th }}$ in class or $33 \approx 18^{\text {th }}$ in whole set Can be implied by diagram indep | May be implied, eg by 21 or 22 or 21.5 <br> Calc'ns need not be correct but need to contain relevant figures for gaining B1B1 $\text { The " } \approx \text { " sign means } \pm 2$ <br> Alternative Method: <br> Ignore comment on skew <br> NB Use EITHER the main method OR the Alternative Method (above), not a mixture of the two. Choose the method that gives most marks. |
| iii | $\geq 3$ mid-pts attempted <br> $\Sigma f x \div 50$ attempted $\quad\left(=\frac{1819}{50}\right)$ <br> $=36.38$ or $36.4(3 \mathrm{sf})$ <br> $\Sigma f x^{2}$ attempted (= 68055.5) $\begin{aligned} & \begin{array}{lr} \sqrt{\frac{68055.5}{50}-\left(\frac{1819}{50}\right)^{2}} & \text { or } \sqrt{1361.11-36.38^{2}} \\ (=\sqrt{37.6056}) \end{array} \\ & =6.13(3 \mathrm{sfs}) \end{aligned}$ <br> Alt for variance: $\begin{array}{ll} \Sigma f(x-\bar{x})^{2}(=1880.28) & \text { M1 } \\ \sqrt{\frac{1880.28}{50}} & \text { M1 } \\ =6.13(3 \mathrm{sf}) & \text { A1 } \end{array}$ | M1 <br> A1 <br> M1 <br> M1 <br> A1 6 | seen or implied <br> $\geq 3$ terms. <br> or 36 with correct working <br> $\geq 3$ terms. <br> completely correct method except midpts \& ft their mean, dep not $\sqrt{ }$ (neg) | Not nec'y correct values ( $29,33,40.5,53$ ) <br> Allow on boundaries. Not class widths <br> Allow on boundaries. Not class widths <br> (3364, 30492, 22963.5, 11236) <br> Allow class widths for this mark only <br> NB mark is not just for "- mean ${ }^{2}$ ", unlike q5(iii) <br> $\Sigma(f x)^{2}:$ M0M0A0 <br> If no wking for $\Sigma f x^{2}$, check using their $x$ and $f$ <br> If no wking or unclear wking: <br> full mks for each correct ans for incorrect ans: $\begin{array}{ll} 35.8 \leq \mu \leq 36.9 & \text { M0M1A0 } \\ 6.0 \leq \text { sd } \leq 6.25 & \text { M1M0A0 } \end{array}$ |
| iv | (a) Decrease <br> (b) Increase <br> (c) Same <br> (d) Same | $\begin{aligned} & \text { B1B1 } \\ & \text { B1B1 } 4 \end{aligned}$ | Ignore other, eg "slightly" or "probably" | Ignore any comments or reasons, even if incorrect |
| Total |  | 16 |  |  |


| 15 | (i) | (a) | $\left(\frac{6}{3}=\right) 2$ | $\begin{aligned} & \text { B1 } \\ & {[1]} \end{aligned}$ | $\left(\frac{6}{9} \times 3=\right) 2$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | (i) | (b) | $\begin{aligned} & 2 / 6 \times 2 \\ & =2 / 3 \text { oe or } 0.667 \text { or } 0.67 \text { or } 0.7 \end{aligned}$ | $\begin{gathered} \text { M1 } \\ \text { A1[2] } \end{gathered}$ | Allow ${ }^{2} 5 \times 2$ or ans 0.8 for M1 | Can be implied, eg $\frac{1}{3}=0.3$, ans 0.6 : M1A0 Allow 0.66 or 0.666 |
|  | (ii) |  | $\begin{aligned} & \hline(3.5,6) \\ & (0.5,0) \text { or }(6.5,15) \end{aligned}$ | $\begin{aligned} & \text { B1 } \\ & \text { B1 } \\ & {[2]} \end{aligned}$ | Ignore incorrect | $(6,3.5)$ AND $(15,6.5):$ B 1 |
|  | (iii) | (a) | $\begin{array}{ll} \frac{\Sigma x f}{21} & \\ =5.43(3 \mathrm{sf}) & \text { or } \frac{114}{21} \text { or } \frac{38}{7} \text { oe } \\ \frac{\Sigma x^{2} f}{21} & \text { or } \frac{817.5}{21} \text { or } 38.9 \ldots \\ & \\ - \text { " } 5.43 "{ }^{2} & \\ (\sqrt{ } 9.4592 \ldots) & \\ =3.08(3 \mathrm{sfs}) & \end{array}$ | M1 <br> A1 <br> M1 <br> M1 <br> A1 <br> [5] | Allow $x$ within classes, incl end pts <br> then $\div 5$ : M0A0 <br> Allow $x$ within class, incl end pt $\div 5$ : M0 <br> dep +ve result; done before $\sqrt{ }$; not $-\left(\bar{x}^{2} \div \ldots\right)$ | $\geq 2$ non-zero terms correct ft their $x$ <br> $\geq 2$ non-zero terms correct ft their $x$ <br> Calc 4 values of $(x-\bar{x})^{2}$ or $(x-\bar{x})^{2} f$ <br> or $(11.8,0.184,6.61,50)$ <br> or $(70.5,1.65,26.4,100)$ or 199 M1 <br> $\frac{\Sigma(x-\bar{x})^{2} f}{21}$ fully correct method M1 |
|  | (iii) | (b) | Actual values or exact hours unknown oe Don't have raw data. oe or measured to nearest hour oe | $\begin{aligned} & \text { B1 } \\ & {[1]} \end{aligned}$ | or Data given in classes or grouped oe or Data evenly distributed in classes oe | Mid-points or medians or averages of class boundaries used oe |

(Q5, Jan 2012)


